

Name: _____

- (5) 1. Define *swamping* in floating point arithmetic.
- (5) 2. Define *digit cancellation* in floating point arithmetic.
- (4) 3. Describe the *machine epsilon* in terms of the distance between neighboring floats.
- (5) 4. State the *Fundamental Axiom of Floating Point Arithmetic*.
- (9) 5. Let $a = 0.0933446$ and $b = 23.26601$. Using 4 decimal digit rounding arithmetic, compute the following:
- (a) $\bar{a} = \text{fl}(a)$
 - (b) $\bar{b} = \text{fl}(b)$
 - (c) What is the relative error in \bar{a} as an approximation to a .

(15) 6. Gauss transforms: let $A \in \mathbb{R}^{n \times n}$ and $m_k \in \mathbb{R}^n$ have 0's in its first k entries.

(a) How many flops are required to compute $B = (I + m_1 e_1^t)A$?

(b) How many flops are required to compute $B = (I + m_k e_k^t)A$?

(c) What is the inverse of $I + m_k e_k^t$? Justify your answer.

(15) 7. Describe how we can use the factorization $A = LU$ to solve the square system $Ax = b$. Give the flop count for your method.

(27) 8. Let $A = \begin{bmatrix} 2 & 1 & 0 \\ -4 & 1 & 2 \\ 2 & 10 & 10 \end{bmatrix}$.

(a) Give L and U from the $A = LU$ factorization of A .

(b) What can be said of the multipliers in Gaussian elimination *with partial pivoting*.

(c) *Why* is pivoting used in Gaussian elimination?

- (8) 9. Solve $Ax = b$, where $PA = LU$ and

$$P = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, \quad L = \begin{bmatrix} 1 & 0 \\ -2 & 1 \end{bmatrix}, \quad U = \begin{bmatrix} 1 & 2 \\ 0 & 2 \end{bmatrix}, \quad \text{and } b = \begin{bmatrix} 2 \\ 1 \end{bmatrix}.$$

- (7) 10. Count the number of flops required to multiply a $n \times n$ lower triangular matrix and an n -vector.